



New2Ans

First, turn the problem "inside-out" by constructing points C', A', and B' using points A, B, and C as radius points and distances AD, BD, and CD as radii. Angle C'-A-B is the same as angle B-A-D, whatever it is. Angle B'-A-C is the same as angle D-A-C also, so angle C'-A-B' is twice angle B-A-C. The same is true for angle B'-C-A' being equal to twice angle A-C-B and angle A'-B-C' being equal to twice angle A-B-C.

In triangle C'-A-B', angles A-C'-B' and A-B'-C' equal  $\frac{1}{2}(180^\circ - 137^\circ 27' 32'')$ , or  $21^\circ 16' 14''$ , so side C'-B' can be solved by:  $(2)(3317.291)\cos 21^\circ 16' 14'' = 6182.620$ .

Triangle B'-C-A' can likewise be solved for side B'-A' by  $(2)(3124.964)\cos 44^\circ 27' 21'' = 4461.139$ , and triangle C'-B-A' can be solved for side C'-A' by  $(2)(2944.009)\cos 24^\circ 16' 25'' = 5367.474$ .

The angles of triangle C'-A'-B' can then be solved by the Law of Cosines:

$$\text{angle } A'C'B' = \arccos \frac{5367.474^2 + 6182.620^2 - 4461.139^2}{(2)(5367.474)(6182.620)} = 44^\circ 45' 10''$$

$$\text{angle } C'A'B' = \arccos \frac{5367.474^2 + 4461.139^2 - 6182.620^2}{(2)(5367.474)(4461.139)} = 77^\circ 21' 04''$$

$$\text{angle } C'B'A' = \arccos \frac{4461.139 + 6182.620^2 - 5367.464^2}{(2)(4461.139)(6182.620)} = 57^\circ 53' 46''$$

Angle A-C'-B =  $21^\circ 16' 14'' + 44^\circ 45' 10'' + 24^\circ 16' 25'' = 90^\circ 17' 49''$  and side AB can be computed by the Law of Cosines:

$$AB^2 = 3317.291^2 + 2944.009^2 - (2)(3317.291)(2944.009)\cos 90^\circ 17' 49'' = 4446.666^2$$

Angle B-A'-C =  $24^\circ 16' 25'' + 77^\circ 21' 04'' + 44^\circ 27' 21'' = 91^\circ 05' 18''$  and side BC can also be computed by the Law of Cosines:

$$BC^2 = 2944.009^2 + 3124.964^2 - (2)(2944.009)(3124.964)\cos 91^\circ 05' 18'' = 5805.274^2$$

and for side AC, angle A-B'-C =  $21^\circ 16' 14'' + 57^\circ 53' 46'' + 44^\circ 27' 21'' = 123^\circ 37' 21''$  and

$$AC^2 = 3317.291^2 + 3124.964^2 - (2)(3317.291)(3124.964)\cos 123^\circ 37' 21'' = 5678.906^2$$