

TestYourself#30Answer

The diameter of the circumcircle can be found from the sides of the triangle by the formula:  
 $2abc/\sqrt{((a+b+c)(-a+b+c)(a-b+c)(a+b-c))}$ , where a,b and c are the sides of the triangle.  
 There are  $6 \times 6 \times 6 = 216$  combinations of the integers 1 to 6 taken three at a time, to wit:

1-1-1	2-1-1	3-1-1	4-1-1	5-1-1	6-1-1
1-1-2	2-1-2	3-1-2	4-1-2	5-1-2	6-1-2
1-1-3	2-1-3	3-1-3	4-1-3	5-1-3	6-1-3
1-1-4	2-1-4	3-1-4	4-1-4	5-1-4	6-1-4
1-1-5	2-1-5	3-1-5	4-1-5	5-1-5	6-1-5
1-1-6	2-1-6	3-1-6	4-1-6	5-1-6	6-1-6
1-2-1	2-2-1	3-2-1	4-2-1	5-2-1	6-2-1
1-2-2	2-2-2	3-2-2	4-2-2	5-2-2	6-2-2
1-2-3	2-2-3	3-2-3	4-2-3	5-2-3	6-2-3
1-2-4	2-2-4	3-2-4	4-2-4	5-2-4	6-2-4
1-2-5	2-2-5	3-2-5	4-2-5	5-2-5	6-2-5
1-2-6	2-2-6	3-2-6	4-2-6	5-2-6	6-2-6
1-3-1	2-3-1	3-3-1	4-3-1	5-3-1	6-3-1
1-3-2	2-3-2	3-3-2	4-3-2	5-3-2	6-3-2
1-3-3	2-3-3	3-3-3	4-3-3	5-3-3	6-3-3
1-3-4	2-3-4	3-3-4	4-3-4	5-3-4	6-3-4
1-3-5	2-3-5	3-3-5	4-3-5	5-3-5	6-3-5
1-3-6	2-3-6	3-3-6	4-3-6	5-3-6	6-3-6
1-4-1	2-4-1	3-4-1	4-4-1	5-4-1	6-4-1
1-4-2	2-4-2	3-4-2	4-4-2	5-4-2	6-4-2
1-4-3	2-4-3	3-4-3	4-4-3	5-4-3	6-4-3
1-4-4	2-4-4	3-4-4	4-4-4	5-4-4	6-4-4
1-4-5	2-4-5	3-4-5	4-4-5	5-4-5	6-4-5
1-4-6	2-4-6	3-4-6	4-4-6	5-4-6	6-4-6
1-5-1	2-5-1	3-5-1	4-5-1	5-5-1	6-5-1
1-5-2	2-5-2	3-5-2	4-5-2	5-5-2	6-5-2
1-5-3	2-5-3	3-5-3	4-5-3	5-5-3	6-5-3
1-5-4	2-5-4	3-5-4	4-5-4	5-5-4	6-5-4
1-5-5	2-5-5	3-5-5	4-5-5	5-5-5	6-5-5
1-5-6	2-5-6	3-5-6	4-5-6	5-5-6	6-5-6
1-6-1	2-6-1	3-6-1	4-6-1	5-6-1	6-6-1
1-6-2	2-6-2	3-6-2	4-6-2	5-6-2	6-6-2
1-6-3	2-6-3	3-6-3	4-6-3	5-6-3	6-6-3
1-6-4	2-6-4	3-6-4	4-6-4	5-6-4	6-6-4
1-6-5	2-6-5	3-6-5	4-6-5	5-6-5	6-6-5
1-6-6	2-6-6	3-6-6	4-6-6	5-6-6	6-6-6

160 can be eliminated as duplicates leaving 56 combinations

21 can be eliminated as impossible triangles (2 sides equal or less than the third side)

All 6 equilateral triangles can be eliminated (Only a 5.4± fits)

Using two of the longest possible sides, 6 & 6, requires a minimum 3rd side of 3.4', thereby eliminating the 22 combinations remaining with a side less than 3 and the 2 greater than/equal to 4 when paired with 6 & 6

The 5 combinations left are computed below showing 5-5-6 to be the correct sides of the triangle

a	b	c	2abc	a+b+c	-a+b+c	a-b+c	a+b-c	sqrt(product)	2abc/sqrt
4	4	5	160	13	5	5	3	31.22498999	5.124101
4	4	6	192	14	6	6	2	31.74901573	6.047432
4	5	5	200	14	6	4	4	36.66060556	5.455447
4	5	6	240	15	7	5	3	39.68626967	6.047432
5	5	6	300	16	6	6	4	48.00000000	6.250000