



Draw lines E-Q1, C-Q1 and Q1-K, perpendicular to EC. Extend Q1-K to AB at N.

BE = EK and KC = CD because they are tangents to Q1 from E and C.

C-Q1-E = 90° because Q1-E and Q1-C bisect supplementary angles.

Q1-K is also the altitude of triangle E-Q1-C, so $[K \cdot (Q1)]^2 = CK \cdot EK$ [1]

Extend BD, CE and FH as shown and drop a perpendicular to FH from Q1 at L.

Mark all known equal angles, noting the ones at Q1 are complementary, making K-Q1-L a right angle and therefore CE ⊥ FH and Q1-K-G-L a square, with side t:

$AC^2 + (AB - EB)^2 = CE^2$, or $s^2 + (s - EB)^2 = (s + EK)^2 = (s + EB)^2$, from which

$$s = 4 \cdot EB, \text{ and } EB = \frac{s}{4}, \text{ so } AE = \frac{3 \cdot s}{4} = EG \text{ and } KG = EG - \frac{s}{4} = \frac{s}{2} = t$$

$$\text{From [1], } t^2 = S \cdot EK = 2 \cdot t \cdot EK, \text{ and } EK = \frac{t}{2} = BE$$

$$AE = EK + KG = \frac{t}{2} + t = \frac{3 \cdot t}{2}$$

$$AC = 2 \cdot t, AE = \frac{3 \cdot AC}{4} \text{ and ACE is a 3:4:5 triangle as are all like it.}$$

$$\text{From } r = \frac{a \cdot b}{a + b + c}$$

$$\text{The radius of Q2} = \frac{\frac{3 \cdot s}{4} \cdot s}{\frac{3 \cdot s}{4} + s + \frac{5 \cdot s}{4}} = \frac{s}{4} \text{ and radius of Q3} = \frac{\frac{2 \cdot s}{3} \cdot \frac{s}{2}}{\frac{s}{2} + \frac{2 \cdot s}{3} + \frac{5 \cdot s}{6}} = \frac{s}{6}$$

$$\text{And their ratio is } \frac{\frac{s}{4}}{\frac{s}{6}} = \frac{2}{3}$$