

Construct BH equal to and parallel with EC.

Construct GH equal to and parallel with AD.

The area of triangle BHG = area of triangle BDG + area triangle GDH + area triangle BDH.

Area of BDH = area EDC = 1/4 area triangle ABC.

Area of GDH = area ADG = 1/4 area triangle ABC.

Area of BDG = 1/4 area of triangle ABC.

Area of BHG = 3/4 area of ABC.

Area of ABC = 4/3 area of BHG.

$$\text{Area of ABC} = \frac{4}{3} \sqrt{m(m-d)(m-e)(m-f)}, \text{ where } m = \frac{d+e+f}{2}$$

For the triangle sides:

$$\overline{AQ}^2 = \overline{AG}^2 + \overline{GQ}^2 - 2 \cdot \overline{AG} \cdot \overline{GQ} \cdot \cos \phi \dots\dots\dots (1)$$

$$\overline{QC}^2 = \overline{GC}^2 + \overline{GQ}^2 - 2 \cdot \overline{CG} \cdot \overline{GQ} \cdot \cos(180^\circ - \phi) \dots\dots\dots (2)$$

$$\cos(180^\circ - \phi) = -\cos \phi \text{ and } AG = GC$$

Expanding and adding (1) & (2),

$$\overline{AQ}^2 + \overline{QC}^2 = \overline{AG}^2 + \overline{GC}^2 + 2 \cdot \overline{GQ}^2, \text{ or } \overline{AQ}^2 + \overline{QC}^2 = 2 \cdot \overline{AG}^2 + 2 \cdot \overline{GQ}^2$$

$$\text{But } AQ = \frac{2}{3} \cdot AD, CQ = \frac{2}{3} \cdot CE, \text{ and } GQ = \frac{1}{3} \cdot GB$$

$$[(2/3)(428.653)]^2 + [(2/3)(342.930)]^2 = (2) \cdot \overline{AG}^2 + (2)[(1/3)(369.976)]^2$$

From which AG = 227.500 and AC = 455.000

Likewise, AB = 482.424 and BC = 380.189

